

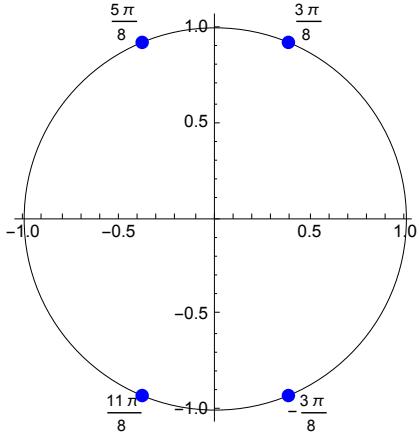
## Equations trigonométriques - Exercices

Résoudre dans  $\mathbb{R}$

- $\sqrt{2} \cos(2x) + 1 = 0$

$$\cos(2x) = -\frac{1}{\sqrt{2}} \iff \cos(2x) = \cos\left(\frac{3\pi}{4}\right)$$

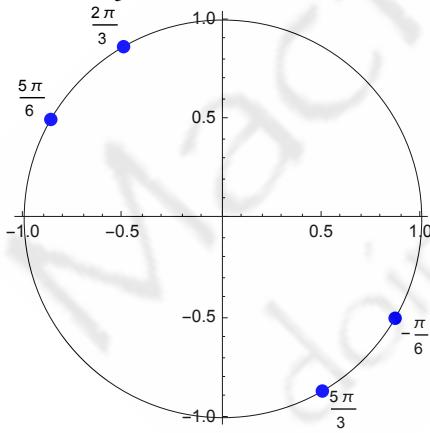
$$\begin{cases} 2x = \frac{3\pi}{4} + 2k\pi & (1) \\ 2x = -\frac{3\pi}{4} + 2k\pi & (2) \end{cases} \iff \begin{cases} x = \frac{3\pi}{8} + k\pi & (1) \\ x = -\frac{3\pi}{8} + k\pi & (2) \end{cases} \quad (k \in \mathbb{Z})$$



- $2 \sin(2x) + \sqrt{3} = 0$

$$\sin(2x) = -\frac{\sqrt{3}}{2} \iff \sin(2x) = \sin\left(-\frac{\pi}{3}\right)$$

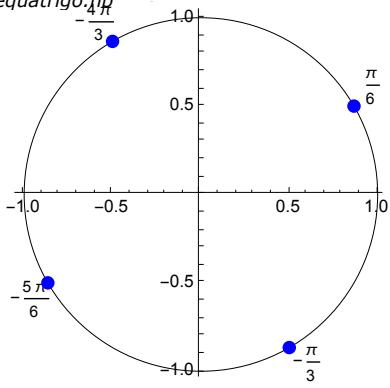
$$\begin{cases} 2x = -\frac{\pi}{3} + 2k\pi & (1) \\ 2x = \frac{4\pi}{3} + 2k\pi & (2) \end{cases} \iff \begin{cases} x = -\frac{\pi}{6} + k\pi & (1) \\ x = \frac{2\pi}{3} + k\pi & (2) \end{cases} \quad (k \in \mathbb{Z})$$



- $\operatorname{tg}\left(2x + \frac{\pi}{3}\right) + \sqrt{3} = 0$

$$\operatorname{tg}\left(\frac{\pi}{3} + 2x\right) = -\sqrt{3} \iff \operatorname{tg}\left(\frac{\pi}{3} + 2x\right) = \operatorname{tg}\left(-\frac{\pi}{3}\right)$$

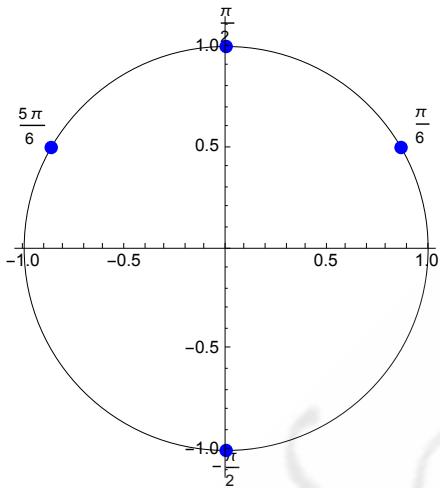
$$\frac{\pi}{3} + 2x = -\frac{\pi}{3} + k\pi \iff x = -\frac{\pi}{3} + \frac{k\pi}{2} \quad (k \in \mathbb{Z})$$



- $\cos(x) = \sin(2x)$

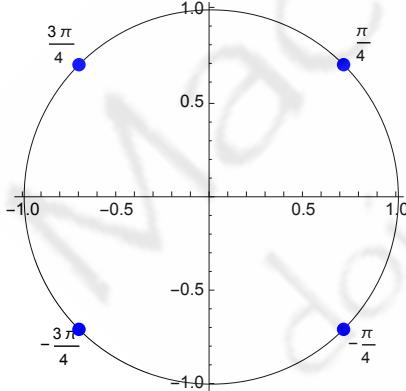
$$\cos(x) = \cos\left(\frac{\pi}{2} - 2x\right)$$

$$\begin{cases} x = \frac{\pi}{2} - 2x + 2k\pi & (1) \\ x = 2x - \frac{\pi}{2} + 2k\pi & (2) \end{cases} \iff \begin{cases} x = \frac{\pi}{6} + \frac{2k\pi}{3} & (1) \\ x = \frac{\pi}{2} - 2k\pi & (2) \end{cases} (k \in \mathbb{Z})$$



- $2\cos^2(x) - 1 = 0$

$$x = \frac{\pi}{4} + k\frac{\pi}{2}$$

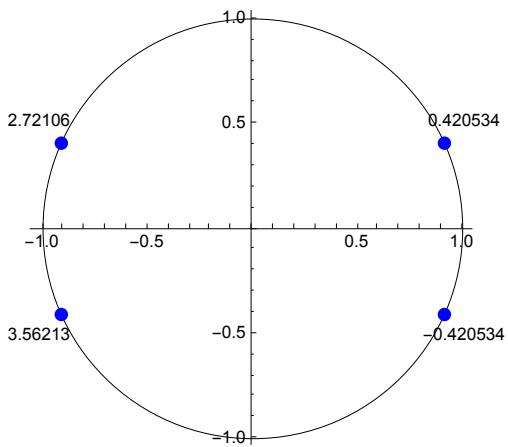


- $3\cos(2x) - 2 = 0$

$$\cos(2x) = \frac{2}{3}$$

$$\begin{cases} 2x = 0.841069 + 2k\pi \\ 2x = -0.841069 + 2k\pi \end{cases}$$

$$\begin{cases} x = 0.420534 + k\pi \\ x = -0.420534 + k\pi \end{cases}$$



- $\operatorname{tg}(3x) = 4$

$$\operatorname{tg}(3x) = \operatorname{tg}(1.32582)$$

$$3x = 1.32582 + k\pi$$

$$x = 0.441939 + k\frac{\pi}{3}$$

